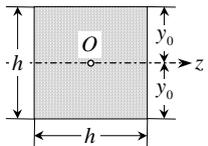
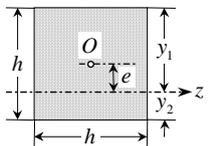
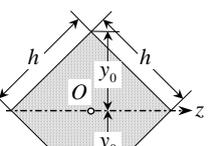
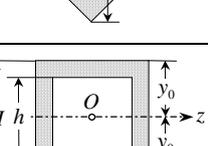
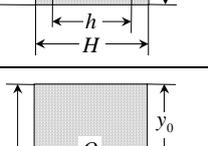
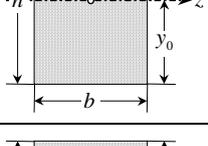
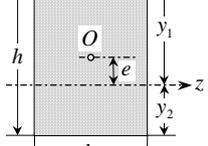
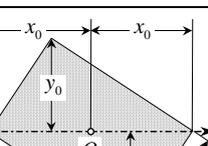
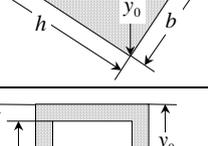


代表的図形の断面諸量 (その1)

	図形	断面積 $A$	図示の軸より縁に至る距離 $y$	図示の軸に関する断面慣性モーメント $I_z$	図示の軸に関する断面係数 $W_z$	図示の軸に関する回転半径 $r_z$
正方形		$h^2$	$y_0 = \frac{h}{2}$	$\frac{h^4}{12}$	$\frac{h^3}{6}$	$\frac{h}{\sqrt{12}} \cong 0.289h$
正方形		$h^2$	$y_1 = \frac{h}{2} + e$ $y_2 = \frac{h}{2} - e$	$\frac{h^4}{12} + h^2 e^2$	$W_1 = \frac{I_z}{y_1} = \frac{h^2(h^2 + 12e^2)}{6(h + 2e)}$ $W_2 = \frac{I_z}{y_2} = \frac{h^2(h^2 + 12e^2)}{6(h - 2e)}$	$\sqrt{\frac{h^2 + 12e^2}{12}}$ $\cong 0.289\sqrt{h^2 + 12e^2}$
正方形		$h^2$	$y_0 = \frac{h}{\sqrt{2}}$ $\cong 0.707h$	$\frac{h^4}{12}$	$\frac{h^3}{6\sqrt{2}} \cong 0.118h^3$	$\frac{h}{\sqrt{12}} \cong 0.289h$
中空正方形		$H^2 - h^2$	$y_0 = \frac{H}{2}$	$\frac{H^4 - h^4}{12}$	$\frac{H^4 - h^4}{6H}$	$\sqrt{\frac{H^2 + h^2}{12}}$ $\cong 0.289\sqrt{H^2 + h^2}$
長方形		$bh$	$y_0 = \frac{h}{2}$	$\frac{bh^3}{12}$	$\frac{bh^2}{6}$	$\frac{h}{\sqrt{12}} \cong 0.289h$
長方形		$bh$	$y_1 = \frac{h}{2} + e$ $y_2 = \frac{h}{2} - e$	$\frac{bh^3}{12} + bhe^2$	$W_1 = \frac{I_z}{y_1} = \frac{bh \cdot (h^2 + 12e^2)}{6(h + 2e)}$ $W_2 = \frac{I_z}{y_2} = \frac{bh \cdot (h^2 + 12e^2)}{6(h - 2e)}$	$\sqrt{\frac{h^2 + 12e^2}{12}}$ $\cong 0.289\sqrt{h^2 + 12e^2}$
長方形		$bh$	$y_0 = \frac{bh}{\sqrt{b^2 + h^2}}$ $x_0 = \frac{\sqrt{b^2 + h^2}}{2}$	$\frac{b^2 h^2}{6(b^2 + h^2)}$	$\frac{b^2 h^2}{6\sqrt{b^2 + h^2}}$	$\frac{bh}{\sqrt{6(b^2 + h^2)}}$
中空長方形		$BH - bh$	$y_0 = \frac{H}{2}$	$\frac{BH^3 - bh^3}{12}$	$\frac{BH^3 - bh^3}{6H}$	$\sqrt{\frac{BH^3 - bh^3}{12(BH - bh)}}$
円		$\frac{\pi d^2}{4}$ $\cong 0.785d^2$	$y_0 = \frac{d}{2}$	$\frac{\pi}{64} d^4 \cong 0.0491d^4$	$\frac{\pi}{32} d^3 \cong 0.0982d^3$	$\frac{d}{4}$

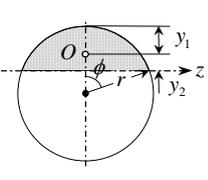
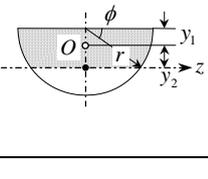
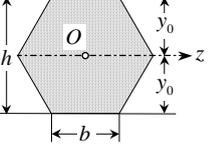
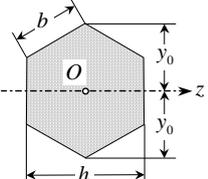
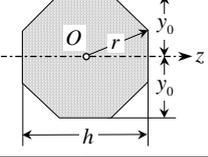
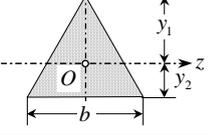
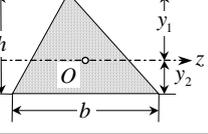
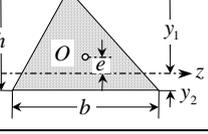
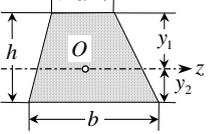
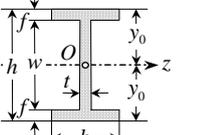
※改訂3版 土木設計便覧, 丸善(1974), pp.1136~1143 に準拠

代表的図形の断面諸量 (その2)

	図形	断面積 $A$	図示の軸より 縁に至る距離 $y$	図示の軸に関する 断面慣性モーメント $I_z$	図示の軸に関する 断面係数 $W_z$	図示の軸に関する 回転半径 $r_z$
円		$\frac{\pi}{4}d^2$ $\cong 0.785d^2$	$y_1 = \frac{d}{2} + e$ $y_2 = \frac{d}{2} - e$	$\frac{\pi}{64}d^4 + \frac{\pi}{4}d^2e^2$	$W_1 = \frac{\pi}{32} \cdot \frac{d^2(d^2 + 16e^2)}{d + 2e}$ $W_2 = \frac{\pi}{32} \cdot \frac{d^2(d^2 + 16e^2)}{d - 2e}$	$\frac{\sqrt{d^2 + 16e^2}}{4}$
中空円		$\frac{\pi}{4}(D^4 - d^4)$	$y_0 = \frac{D}{2}$	$\frac{\pi}{64}(D^4 - d^4)$ $\cong 0.0491(D^4 - d^4)$	$\frac{\pi}{32} \cdot \frac{D^4 - d^4}{D}$ $\cong 0.0982 \frac{D^4 - d^4}{D}$ $\cong 0.8D^2t$ <i>t/D が小さいとき</i>	$\sqrt{\frac{D^2 + d^2}{4}}$
半円		$\frac{\pi}{8}d^2$ $\cong 0.393d^2$	$y_1 = \frac{3\pi - 4}{6\pi}d$ $\cong 0.288d$ $y_2 = \frac{2}{3\pi}d$ $\cong 0.212d$	$\frac{9\pi^2 - 64}{1152\pi}d^4$ $\cong 0.00686d^4$	$W_1 = \frac{9\pi^2 - 64}{192(3\pi - 4)}d^3$ $\cong 0.0239d^3$ $W_2 = \frac{9\pi^2 - 64}{768}d^3$ $\cong 0.0325d^3$	$\frac{\sqrt{9\pi^2 - 64}}{12\pi}d$ $\cong 0.132d$
半円		$\frac{\pi}{8}d^2$ $\cong 0.393d^2$	$y_1 = \frac{2}{3\pi}d$ $\cong 0.212d$ $y_2 = \frac{3\pi - 4}{6\pi}d$ $\cong 0.288d$	$\frac{1}{16} \cdot \left(\frac{5}{8}\pi - \frac{4}{3}\right) \cdot d^4$ $\cong 0.0394d^4$	$W_1 = \frac{I_z}{y_1}, W_2 = \frac{I_z}{y_2}$	$\sqrt{\frac{5}{16} - \frac{2}{3\pi}}d$ $\cong 0.317d$
中空半円		$\pi r_0 t$	$y_1 = \left(1 - \frac{2}{\pi}\right) \cdot r_0 + \frac{t}{2}$ $y_2 = \frac{2}{\pi}r_0$	$\left(\frac{\pi}{2} - \frac{4}{\pi}\right) \cdot r_0^3 t$ $\cong 0.298r_0^3 t$	$W_1 = \frac{I_z}{y_1}, W_2 = \frac{I_z}{y_2}$	$\sqrt{\frac{1}{2} - \frac{4}{\pi^2}}r_0$ $\cong 0.308r_0$
楕円		$\frac{\pi ab}{4}$ $\cong 0.785ab$	$y_0 = \frac{a}{2}$	$\frac{\pi}{64}a^3b \cong 0.0491a^3b$	$\frac{\pi}{32}a^2b \cong 0.0982a^2b$	$\frac{a}{4}$
中空楕円		$\frac{\pi}{4}(HB - hb)$ $\cong 0.785$ $\times (HB - hb)$	$y_0 = \frac{H}{2}$	$\frac{\pi}{64}(H^3B - h^3b)$ $\cong 0.0491$ $\times (H^3B - h^3b)$	$\frac{\pi}{32} \cdot \frac{H^3B - h^3b}{H}$ $\cong 0.0982 \cdot \frac{H^3B - h^3b}{H}$	$\frac{1}{4} \sqrt{\frac{H^3B - h^3b}{HB - hb}}$
小判型		$\frac{\pi}{4}d^2 + hd$	$y_0 = \frac{h + d}{2}$	$\frac{\pi d^4}{64} + \frac{hd^3}{6}$ $+$ $\frac{\pi h^2 d^2}{16} + \frac{h^3 d}{12}$	$W = \frac{I_z}{y_0}$	$r_z = \sqrt{\frac{I_z}{A}}$
中空小判型		$2(\pi r_0 + h)t$	$y_0 = r_0 + \frac{h + t}{2}$	$\pi t r_0^3 + 4t r_0^2 h$ $+$ $\frac{\pi}{2} t r_0 h^2 + \frac{1}{6} t h^3$	$W = \frac{I_z}{y_0}$	$r_z = \sqrt{\frac{I_z}{A}}$

※改訂3版 土木設計便覧, 丸善(1974), pp.1136~1143 に準拠

代表的図形の断面諸量 (その3)

図形	断面積 $A$	図示の軸より縁に至る距離 $y$	図示の軸に関する断面慣性モーメント $I_z$	図示の軸に関する断面係数 $W_z$	図示の軸に関する回転半径 $r_z$
欠円	 $\frac{r^2}{2}(2\phi - \sin 2\phi)$	$y_1 = r(1 - \cos \phi) - y_2$ $y_2 = \frac{2\left[\frac{1}{3}\sin \phi(2 + \cos^2 \phi) - \phi \cos \phi\right]}{2\phi - \sin 2\phi}r$	$r^4 \left[ \phi \left( \frac{1}{4} + \cos^2 \phi \right) - \sin \phi \cos \phi \left( \frac{5}{4} - \frac{1}{6} \sin^2 \phi \right) \right]$		$r_z = \sqrt{\frac{I_z}{A}}$
円帯	 $\frac{r^2}{2}(2\phi + \sin 2\phi)$	$y_1 = r \sin \phi - y_2$ $y_2 = \frac{2\left[\frac{1}{3}\sin \phi(2 + \cos^2 \phi) + \left(\frac{\pi}{2} - \phi\right)\cos \phi - \frac{2}{3}\right]}{2\phi + \sin 2\phi}r$	$r^4 \left[ \left( \frac{\pi}{2} - \phi \right) \left( \frac{1}{4} + \cos^2 \phi \right) + \sin \phi \cos \phi \left( \frac{5}{4} - \frac{1}{6} \sin^2 \phi \right) \right]$		$r_z = \sqrt{\frac{I_z}{A}}$
正六角形	 $\frac{\sqrt{3}}{2}h^2$ $\cong 0.866h^2$ $\frac{3\sqrt{3}}{2}b^2$ $\cong 2.598b^2$	$y_0 = \frac{h}{2}$	$\frac{5\sqrt{3}}{144}h^4 \cong 0.0602h^4$ $\frac{5\sqrt{3}}{16}b^4 \cong 0.541b^4$	$\frac{5\sqrt{3}}{72}h^3 \cong 0.120h^3$ $\frac{5}{8}b^3 = 0.625b^3$	$\sqrt{\frac{5}{72}}h \cong 0.264h$ $\sqrt{\frac{5}{24}}b \cong 0.456b$
正六角形	 $\frac{\sqrt{3}}{2}h^2$ $\cong 0.866h^2$ $\frac{3\sqrt{3}}{2}b^2$ $\cong 2.598b^2$	$y_0 = \frac{h}{\sqrt{3}} \cong 0.577h$	$\frac{5\sqrt{3}}{144}h^4 \cong 0.0602h^4$ $\frac{5\sqrt{3}}{16}b^4 \cong 0.541b^4$	$\frac{5}{48}h^3 \cong 0.104h^3$ $\frac{5\sqrt{3}}{16}b^3 \cong 0.541b^3$	$\sqrt{\frac{5}{72}}h \cong 0.264h$ $\sqrt{\frac{5}{24}}b \cong 0.456b$
正八角形	 $2h^2 \tan 22.5^\circ$ $\cong 0.828h^2$ $4r^2 \sin 45^\circ$ $\cong 2.828r^2$	$r \cos 22.5^\circ$ $\cong 0.924r$	$0.0547h^4$ $0.638r^4$	$0.109h^3$ $0.691r^3$	$0.257h$ $0.475r$
正三角形	 $\frac{\sqrt{3}}{4}b^2$ $\cong 0.433b^2$	$y_1 = \frac{\sqrt{3}}{3}b \cong 0.577b$ $y_2 = \frac{\sqrt{3}}{6}b \cong 0.289b$	$\frac{b^4}{32\sqrt{3}} \cong 0.0180b^4$	$W_1 = \frac{I_z}{y_1} = \frac{b^3}{32}$ $W_2 = \frac{I_z}{y_2} = \frac{b^3}{16}$	$\frac{b}{\sqrt{24}} \cong 0.204b$
三角形	 $\frac{bh}{2}$	$y_1 = \frac{2}{3}h$ $y_2 = \frac{1}{3}h$	$\frac{bh^3}{36}$	$W_1 = \frac{I_z}{y_1} = \frac{bh^2}{24}$ $W_2 = \frac{I_z}{y_2} = \frac{bh^2}{12}$	$\frac{h}{\sqrt{18}} \cong 0.236h$
三角形	 $\frac{bh}{2}$	$y_1 = \frac{2}{3}h + e$ $y_2 = \frac{1}{3}h - e$	$\frac{bh}{36}(h^2 + 18e^2)$	$W_1 = \frac{I_z}{y_1}$ $W_2 = \frac{I_z}{y_2}$	$\sqrt{\frac{h^2 + 18e^2}{18}}$
台形	 $\frac{(a+b)h}{2}$	$y_1 = \frac{a+2b}{a+b} \times \frac{h}{3}$ $y_2 = \frac{2a+b}{a+b} \times \frac{h}{3}$	$\frac{a^2 + 4ab + b^2}{36(a+b)}h^3$	$W_1 = \frac{a^2 + 4ab + b^2}{12(a+2b)}h^2$ $W_2 = \frac{a^2 + 4ab + b^2}{12(2a+b)}h^2$	$\frac{\sqrt{2(a^2 + 4ab + b^2)}}{6(a+b)}h$
I形	 $bh - w(b-t)$	$y_0 = \frac{h}{2}$	$\frac{bh^3 - w^3(b-t)}{12}$	$\frac{bh^3 - w^3(b-t)}{6h}$	$\frac{\sqrt{bh^3 - w^3(b-t)}}{\sqrt{12[bh - w(b-t)]}}$

代表的図形の断面諸量（その4）

	図形	断面積 $A$	図示の軸より 縁に至る距離 $y$	図示の軸に関する 断面慣性モーメント $I_z$	図示の軸に関する 断面係数 $W_z$	図示の軸に関する 回転半径 $r_z$
I形		$bh - w(b-t)$	$y_0 = \frac{b}{2}$	$\frac{2fb^3 + wt^3}{12}$	$\frac{2fb^3 + wt^3}{6b}$	$\sqrt{\frac{2fb^3 + wt^3}{12[bh - w(b-t)]}}$
溝形		$bh - w(b-t)$	$y_0 = \frac{h}{2}$	$\frac{bh^3 - w^3(b-t)}{12}$	$\frac{bh^3 - w^3(b-t)}{6h}$	$\sqrt{\frac{bh^3 - w^3(b-t)}{12[bh - w(b-t)]}}$
溝形		$bh - w(b-t)$	$y_1 = \frac{b^2h - w(b-t)^2}{2[bh - w(b-t)]}$ $y_2 = b - y_1$	$\frac{2fb^3 + wt^3}{12} - Ay_2^2$	$W_1 = \frac{I_z}{y_1}$ $W_2 = \frac{I_z}{y_2}$	$r_z = \sqrt{\frac{I_z}{A}}$
十字形		$at + f(b-t)$	$y_0 = \frac{a}{2}$	$\frac{ta^3 + f^3(b-t)}{12}$	$\frac{ta^3 + f^3(b-t)}{6a}$	$\sqrt{\frac{ta^3 + f^3(b-t)}{12[at + f(b-t)]}}$
T形		$bf + wt$	$y_1 = \frac{th^2 + f^2(b-f)}{2(bf + wt)}$ $y_2 = h - y_1$	$\frac{th^3 + (b-t)f^3}{3} - Ay_1^2$	$W_1 = \frac{I_z}{y_1}$ $W_2 = \frac{I_z}{y_2}$	$r_z = \sqrt{\frac{I_z}{A}}$
T形		$bf + \frac{w}{2}(t_1 + t_2)$	$y_1 = \frac{3bf^2 + 3t_2w(b+f) + w(t_1-t_2)(3f+w)}{6A}$ $y_2 = h - y_1$	$\frac{4bf^3 + w^3(t_1 + 3t_2)}{12} - A(y_1 - f)^2$	$W_1 = \frac{I_z}{y_1}$ $W_2 = \frac{I_z}{y_2}$	$r_z = \sqrt{\frac{I_z}{A}}$
T形 (変形)		$Bf_1 + wt + bf_2$	$y_1 = \frac{h^2t + (b-t)f_1^2 + (b-t)(2h-f_2)f_2}{2A}$ $y_2 = h - y_1$	$\frac{1}{3} \begin{bmatrix} By_1^3 + by_2^3 \\ -(B-t)(y_1 - f_1)^3 \\ -(b-t)(y_2 - f_2)^3 \end{bmatrix}$	$W_1 = \frac{I_z}{y_1}$ $W_2 = \frac{I_z}{y_2}$	$r_z = \sqrt{\frac{I_z}{A}}$
放物線形		$\frac{2}{3}BH$	$\frac{H}{2}$	$\frac{BH^3}{30}$	$\frac{BH^2}{15}$	$\frac{H}{2\sqrt{5}}$
放物線形		$\frac{2}{3}BH$	$y_1 = \frac{2}{5}H$ $y_2 = \frac{3}{5}H$	$\frac{8}{175}BH^3$	$W_1 = \frac{I_z}{y_1} = \frac{4}{35}BH^2$ $W_2 = \frac{I_z}{y_2} = \frac{8}{105}BH^2$	$\sqrt{\frac{12}{175}}H$
放物線形		$\frac{2}{3}BH$	$y_1 = \frac{3}{8}H$ $y_2 = \frac{5}{8}H$	$\frac{19}{480}BH^3$	$W_1 = \frac{I_z}{y_1} = \frac{19}{180}BH^2$ $W_2 = \frac{I_z}{y_2} = \frac{19}{300}BH^2$	$\frac{\sqrt{95}}{40}H$

※改訂3版 土木設計便覧, 丸善(1974), pp.1136~1143に準拠